

# Ratios, Rates and Proportions

Name: \_\_\_\_\_

Date: \_\_\_\_\_

## Concepts

- Ordering Rational Numbers
- Percentages and Directly Proportional Situations
- Proportional Situations (theory)
- Proportions
- Rates
- Rational Numbers ( $\mathbb{Q}$ )
- Ratios
- Recognizing a Directly or Inversely Proportional Situation
- Solving Directly or Inversely Proportional Situations
- Translating a Situation Into a Ratio or Rate

## Ordering Rational Numbers

1. At a Saguenay ski hill, a technician records how each of five snow markers has changed since last week, in centimetres. A positive value means the snow got deeper.

a) Marker A:  $+\frac{3}{4}$    Marker B:  $-1.5$    Marker C:  $-\frac{1}{2}$    Marker D:  $+2.25$    Marker E:  $-\frac{9}{4}$

Write the five values in order from least to greatest.

b) Which marker changed the least, that is, which value sits closest to zero?

c) Which markers lost more than 1 cm of snow?

**Percentages and Directly Proportional Situations**

2. A Secondary 1 class in Trois-Rivières is selling tickets for a spaghetti supper.
- a) By Monday evening they had sold 45 tickets, which their teacher says is 15% of the goal. How many tickets is the goal?
  - b) By Friday they had sold 240 tickets. What percentage of the goal is that?
  - c) How many more tickets must they sell to reach the goal?

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**Proportional Situations**

3. For each pair of quantities below, decide whether the situation is *proportional* or *not proportional*, and give a one-sentence reason.
- a) The number of hockey pucks bought and the total cost, at \$4 per puck.
  - b) A student's age and their height.
  - c) The number of hours a tap runs at a steady flow and the number of litres it delivers.
  - d) The side length of a square and its perimeter.
  - e) The side length of a square and its area.

**Proportions**

4. To mix her school's team colour, an art teacher uses 5 mL of blue paint for every 8 mL of white paint.
- a) She wants to use up a full 200 mL bottle of white. Set up a proportion and find how much blue she needs.
  - b) How much paint will the finished mixture contain in total?
  - c) On another day she has only 35 mL of blue left. How much white should she use to get the same colour?

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**Rates**

5. A dépanneur sells the same granola bars in three box sizes:

| Box    | Bars | Price   |
|--------|------|---------|
| Small  | 6    | \$7.20  |
| Medium | 10   | \$11.50 |
| Large  | 24   | \$28.80 |

- a) Find the unit rate — the price per bar — for each box.
- b) Which box gives the best value? Is it the one you expected?
- c) How much does a student save by buying 30 bars as three medium boxes rather than as five small boxes?

**Rational Numbers ( $\mathbb{Q}$ )**

**6.** A rational number is any number that can be written as a fraction whose numerator and denominator are integers, with the denominator not zero. Show that each number below is rational by writing it as a fraction in lowest terms.

- a) 0.35
- b) 6
- c) 45%
- d)  $2\frac{1}{4}$
- e)  $\frac{18}{24}$

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**Ratios**

**7.** A community garden in Rosemont divides its plots between vegetables and flowers in the ratio 7 : 3.

- a) There are 210 plots in all. How many are vegetable plots and how many are flower plots?
- b) Write the ratio of flower plots to vegetable plots.
- c) The next spring, 21 flower plots are added and no vegetable plots. Write the new vegetable : flower ratio in simplest form.

**Recognizing a Directly or Inversely Proportional Situation**

**8.** For each situation, state whether the two quantities are *directly* proportional, *inversely* proportional, or *neither*, and justify with a calculation or a sentence.

a) Volunteers painting an arena:

|                      |    |    |    |    |
|----------------------|----|----|----|----|
| Number of volunteers | 2  | 3  | 6  | 12 |
| Hours to finish      | 36 | 24 | 12 | 6  |

b) The number of litres of gas put in a tank and the amount paid, at a fixed price per litre.

c) The length of one side of a rectangle whose area is fixed at  $48 \text{ cm}^2$ , and the length of the side next to it.

d) The outdoor temperature and the number of hot chocolates sold at a ski chalet.

**Solving Directly or Inversely Proportional Situations**

**9.** A summer camp on Île d'Orléans has enough food to feed 24 campers for 15 days. The food supply is fixed.

- a) Are the number of campers and the number of days directly or inversely proportional? Explain in one sentence.
- b) Find the constant of the situation and say what it measures.
- c) If 40 campers show up instead of 24, how many days will the food last?

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**Translating a Situation Into a Ratio or Rate**

**10.** For each situation, write the comparison that is asked for, say whether it is a *ratio* or a *rate*, and justify your choice using the units.

- a) A bag of trail mix holds 120 g of almonds and 200 g of raisins. Compare almonds to raisins.
- b) A coach bus covers 150 km in 2 hours. Compare distance to time.
- c) A dance class has 18 girls and 12 boys. Compare the boys to the whole class.
- d) A printer produces 45 pages in 3 minutes. Compare pages to minutes.

**Synthesis — drawing on several sheets in this topic**

**11.** A bubble-tea shop on rue Wellington records one Saturday. It sold 3 large teas for every 5 small teas, 320 teas in all. A large costs \$6.50 and a small costs \$4.00, and all 320 were served over a 4-hour rush.

- a) How many large teas and how many small teas were sold?
- b) What percentage of the teas sold were large?
- c) What were the shop's total takings for the rush?
- d) Express the sales as a rate in teas per hour, and use that rate to say how many teas the shop serves in 15 minutes.

**Want the harder problems and the worked solutions?**

The *Challenge Problems* set and the *Answer Keys* for Ratios, Rates and Proportions — with the reasoning written out in full — are available at [tutorinmontreal.ca](http://tutorinmontreal.ca).