

Perimeter, Area and Units of Measurement

Name: _____

Date: _____

Concepts

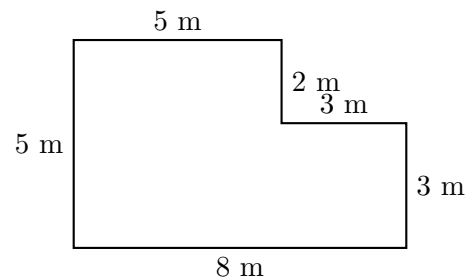
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Constructing a Circle

1. Zoe opens her compass to 4.5 cm and draws a circle on her poster.
 - a) Give the radius and the diameter of her circle.
 - b) She then draws a chord that measures exactly 9 cm. What is this chord called, and explain why no chord of her circle can be longer than 9 cm.
 - c) Find the circumference of the circle, first as an exact multiple of π and then as a decimal (use $\pi \approx 3.14$).

Decomposable Geometric Figures

2. The floor of a storage room at an arena is shaped like the letter L.



- Describe two *different* ways of cutting this floor into rectangles, giving the dimensions of each piece.
- Find the area of the floor with both of your decompositions, and check that they agree.
- The segment you drew to cut the figure does not appear anywhere in the perimeter of the room. Explain why.

Finding Missing Measurements in Plane Figures From the Perimeter**3.**

- a) An isosceles triangular banner has a perimeter of 74 cm. Its base measures 24 cm. Find the length of each of the two equal sides.
- b) A rectangular window has a perimeter of 74 cm and a width of 16 cm. Find its length.
- c) In one sentence, say what is the same about the first step of the two solutions.

Methods to Decompose Figures

- 4. A workshop tabletop is a rectangle 120 cm long and 80 cm wide, with a semicircular bite of diameter 80 cm cut out of one of the short ends.
 - a) Would you find this area by *addition* (cutting into pieces) or by *subtraction* (removing a piece from a bigger figure)? Say why.
 - b) Find the area of the tabletop, to the nearest square centimetre. Use $\pi \approx 3.14$.

Missing Measurements in Plane Figures

5. For each situation below, first say whether the measurement you are given is a *perimeter* or an *area*, then name the relation you will undo, and only then find the missing measurement.

- a) A parallelogram has an area of 96 cm^2 and a base of 12 cm. Find its height.
- b) A rectangle has a perimeter of 30 cm and a length of 9 cm. Find its width.
- c) A triangle has an area of 45 cm^2 and a height of 9 cm. Find its base.

The Arcs and Sectors of a Circle

6. A round pizza of radius 18 cm is cut into slices. One slice is a sector with a central angle of 40° . Give each answer as an exact multiple of π and then as a decimal, using $\pi \approx 3.14$.

- a) Find the length of the crust on that slice (the arc).
- b) Find the area of the slice.
- c) Find the perimeter of the slice. Be careful — it is not the same as your answer to (a).

The Area and the Perimeter of Triangles

7. A triangular flower bed sits in the corner of a park. Its three sides measure 9 m, 12 m and 15 m, and the corner where the 9 m and 12 m sides meet is a right angle.

- a) Find the area of the flower bed.
- b) Find its perimeter.
- c) Metal edging costs \$8.50 per metre. Find the cost of edging the whole bed.

The Perimeter and The Area of Decomposable Figures

8. A community-centre window is shaped like a rectangle 2.4 m wide and 1.8 m tall with a semicircle sitting on top of it, the flat side of the semicircle being the top of the rectangle. Use $\pi \approx 3.14$ and round each answer to the nearest hundredth.

- a) Find the area of the glass.
- b) Find the perimeter of the window frame that goes round the outside of the glass.

The Perimeter and the Area of Plane Figures

- 9.** Read each set of measurements carefully — one of them mixes two units.
- a) A toy kite is shaped like a rhombus. Its diagonals measure 48 cm and 0.2 m, and each of its four sides measures 26 cm. Find its area and its perimeter, in centimetres.
 - b) A wooden deck is a trapezoid. Its two parallel sides measure 10 m and 4 m, the distance between them is 4 m, and its two slanted sides each measure 5 m. Find its area and its perimeter.

The Perimeter and the Area of Quadrilaterals

- 10.** A parallelogram-shaped banner has a base of 1.2 m. Its two slanted sides each measure 60 cm, and the perpendicular distance between the base and the side opposite it is 45 cm.
- a) Find the area of the banner in cm^2 .
 - b) Find its perimeter, in centimetres and then in metres.
 - c) The 60 cm slanted side is not the number used in the area formula. Explain why not.

The Perimeter and the Area of Regular Polygons — Secondary 1 and 2**11.**

- a) A paving stone is a regular hexagon with sides of 8 cm and an apothem of 6.9 cm. Find its perimeter and its area.
- b) A blank metal plate is a regular octagon with sides of 15 cm and an apothem of 18.1 cm. Find its perimeter and its area.
- c) In your own words, say what the apothem of a regular polygon is.

Units for Measuring Mass and Their Conversion

12. A factory packs granola bars. Each bar has a mass of 45 g, a carton holds 24 bars, and the empty carton itself has a mass of 180 g.

- a) Find the mass of a full carton, in grams and then in kilograms.
- b) A pallet holds 500 full cartons. Find its mass in kilograms and then in tonnes.
- c) A vitamin tablet has a mass of 250 mg. How many tablets would it take to match the mass of one granola bar?

Units of Length**13.**

- a) Put these five lengths in order from smallest to largest, converting them all to metres first: 4500 mm, 0.004 km, 45 cm, 4.5 dm, 0.9 m. Two of them are equal — say which.
- b) A hallway is 12.5 m long. Floor tiles are 25 cm wide. How many tiles fit in one row along the hallway?

Units of Time and Their Conversion**14.**

- a) Convert 2 h 45 min to minutes, and convert 500 s to minutes and seconds.
- b) A hockey tournament starts its first game at 8:15. Each game lasts 1 h 25 min, and the ice is resurfaced for 10 min between games. At what time does the third game end?

Synthesis — drawing on several sheets in this topic

15. A new concrete skatepark pad is a rectangle 12 m by 7 m, with one corner rounded off: a quarter-circle of radius 4 m has been cut away from that corner. Use $\pi \approx 3.14$.

- a) Find the area of the pad, to the nearest hundredth of a square metre.
- b) Find the perimeter of the pad, to the nearest hundredth of a metre.
- c) Rubber edging is sold only in straight 2.5 m lengths that can be bent round the curve. How many lengths must the town buy?

Want the harder problems and the worked solutions?

The *Challenge Problems* set and the *Answer Keys* for Perimeter, Area and Units of Measurement — with the reasoning written out in full — are available at tutorinmontreal.ca.